SciQL, Bridging the Gap between Science and Relational DBMS

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ABSTRACT

Scientific discoveries increasingly rely on the ability to efficiently grind massive amounts of experimental data using database technologies. To bridge the gap between the needs of the Data-Intensive Research fields and the current DBMS technologies, we propose SciQL (pronounced as 'cycle'), the first SQL-based query language for scientific applications with both tables and arrays as first class citizens. It provides a seamless symbiosis of array-, set- and sequence-interpretations. A key innovation is the extension of value-based grouping of SQL:2003 with structural grouping, i.e., fixed-sized and unbounded groups based on explicit relationships between elements positions. This leads to a generalisation of window-based query processing with wide applicability in science domains. This paper describes the main language features of SciQL and illustrates it using time-series concepts.

Categories and Subject Descriptors

E.1 [Data Structures]: Arrays; H.2.3 [Languages]: Query languages; H.2.8 [Database Applications]: Scientific databases

General Terms

Language

Keywords

SciQL, array query language, array database, scientific databases, time series

1. INTRODUCTION

The array computational paradigm is prevalent in most sciences and it has drawn attention from the database research community for many years. The object-oriented database systems of the '90s allowed any collection type to be used recursively [4] and multidimensional database systems took it as the starting point for their design [21]. The hooks provided in relational systems for user defined functions and data types create a stepping stone towards interaction with array-based libraries, i.e. RasDaMan [6] is one of the few systems in this area that have matured beyond the laboratory stage. Nevertheless, the array paradigm taken in isolation is insufficient to create a full-fledged scientific information system. Such a system should blend measurements with static and derived metadata about the instruments and observations. It therefore calls for a strong symbiosis of the relational paradigm and array paradigm. The SciQL language presented in this paper fills this gap.

The mismatch between application needs and database technology has a long history, e.g., [22, 8, 55, 20, 23, 21]. The main problems encountered with relational systems in science can be summed up as (i) the impedance mismatch between query language and array manipulation, (ii) the difficulty to write complex array-based expressions in SQL, (iii) Arrays are not first class citizens, and (iv) ingestion of terabytes of data is too slow. The traditional DBMS simply carries too much overhead. Moreover, much of the science processing involves use of standard libraries, e.g., LINPACK, and statistics tools, e.g., R. Their interaction with a database is often confined to a simplified data import/export facility. The proposed standard for management of external data (SQL3/MED) [42] has not materialised as a component in contemporary system offerings.

A query language is needed that achieves a true symbiosis of the TABLE and ARRAY semantics in the context of existing external software libraries. This led to the design of SciQL, where arrays are made first class citizens by enhancing the SQL:2003 framework along three innovative lines:

- **Seamless integration** of array-, set-, and sequence-semantics.
- **Named dimensions with constraints** as a declarative means for indexed access to array cells.
- **Structural grouping** to generalize the value-based grouping towards selective access to groups of cells based on positional relationships for aggregation.

A TABLE and an ARRAY differ semantically in a straightforward manner. A TABLE denotes a (multi-) set of tuples, while an ARRAY denotes a (sparsely) indexed collection of tuples called **cells**. All cells covered by an array’s dimensions always exist **conceptually** and their non-dimensional attributes are initialised to a default value, while in a TABLE tuples only come into existence after an explicit insert operation. Arrays may appear wherever tables are allowed in an SQL expression, producing an array if the column list of a SELECT statement contains dimensional expressions. The SQL iterator semantics associated with TABLES carry over to ARRAYS, but iteration is confined to cells whose non-dimensional attributes are not NULL.

An important operation is to carve out an array slab for further processing. The windowing scheme in SQL:2003 is a step into this
2. LANGUAGE MODEL

In this section we summarize the features offered in SciQL concerning ARRAY definition, instantiation and modification, as well as coercions between TABLE and ARRAY.

2.1 Array Definitions

We purposely stay as close as possible to the syntax and semantics of SQL:2003. An array object definition reuses the syntax of table with a few minor additions. An array has one or more dimensional attributes (for short: dimensions) and zero or more non-dimensional attributes. A dimension is a measurement of the size of the array in a particular named direction, e.g., “x”, “y”, “z” or “time”. A dimensional attribute is denoted by the keyword DIMENSION with optional constraints describing the dimension range. The data type of a dimension can be any of the basic scalar data types, including TIMESTAMP, FLOAT and VARCHAR. The non-dimensional attributes of an array can be of any data types a normal table column can be and they may use a DEFAULT clause to initialize their values. The default value may be arbitrarily taken from a scalar expression, a cell’s dimensional value(s) (i.e., the cell’s coordinates on the array dimensions) or a side-effect free function. Omission of the default or assignment of a NULL-value produces a ‘hole’, which is ignored by the built-in aggregation functions.

Arrays are either fixed or unbounded. An array is fixed iff all its dimensions are fixed, otherwise it is unbounded. The range and size of a fixed dimension are exactly specified using the sequence pattern `[<start>..<stop>]<size>], which is composed out of expressions each producing one scalar value. The interval between start and stop has an open end-point, i.e., stop is not included. For integer dimensions, the traditional syntax using an integer upper bound `[size>] is allowed as a shortcut of the sequence pattern [0:1:<size>]. Figure 1 shows four fixed arrays with different forms. In addition to the most common C-style rectangular arrays (Fig.1-a), stripes (Fig.1-b) can be defined as one where the default value of some rows is indistinguishable from out of bound access, i.e., those cells are explicitly excluded by carrying NULL values in their non-dimensional attributes. A diagonal array (Fig.1-c) is easily formulated using a predicate over the dimensions involved. It is even possible to carve out an array based on its content (Fig.1-d), thereby effectively nullifying all cells outside the domain of validity and producing a sparse array. This feature is of particular interest to remove outliers using an integrity constraint. Evidently, different array forms can lead to very different considerations with respect to their physical representation, a topic discussed in a companion paper.

The SQL update semantics is extended towards arrays in a straightforward manner. The array cells are initialised upon creation with

```sql
CREATE ARRAY matrix | 
  x INT DIMENSION[4],
  y INT DIMENSION[4],
  v FLOAT DEFAULT 0.0 |
);

CREATE ARRAY stripes | 
  x INT DIMENSION[4],
  y INT DIMENSION[4] CHECK(MOD(y,2) = 1),
  v FLOAT DEFAULT 0.0 |
);

CREATE ARRAY diagonal | 
  x INT DIMENSION[4],
  y INT DIMENSION[4] CHECK(x = y),
  v FLOAT DEFAULT 0.0 |
);

CREATE ARRAY sparse | 
  x INT DIMENSION[4],
  y INT DIMENSION[4],
  v FLOAT DEFAULT 0.0 CHECK(v BETWEEN 0 AND 10) |
);
```

A dimension is unbounded if any of its start, step, or stop expressions is identified by the pseudo expression ‘*’. A DIMENSION clause without a sequence pattern implies the most open pattern ‘*[<*>:*]’. Cells in an unbounded array can be modified using the INSERT and DELETE statements carried over from the table semantics. An unbounded array has an implicitly defined actual size derived from the minimal bounding rectangle that encloses all cells with an explicitly inserted non-NULL value in the array. When walking through an array instance, cells outside the minimal bounding rectangle are ignored. However, direct access to any cells within the array’s dimension bounds is guaranteed to produce the default value. The effect is that listing an array with unbounded dimensions still produces a finite result, but it may be huge. An unbounded dimension is typically used for an n-dimensional spatial array where only part of the dimension range designates a non-empty array cell. Time series are also prototypical examples of arrays with unbounded dimensions.

2.2 Array Modifications

The SQL update semantics is extended towards arrays in a straightforward manner. The array cells are initialised upon creation with

```
Figure 1: SciQL fixed arrays with different forms

[Table showing fixed arrays with different forms]

Figure 2: Results of updating the four fixed arrays by the first four queries in Section 2.2.

[Table showing results of updating fixed arrays]

Direction. It was primarily introduced to better handle time series in business data warehouses and data mining. In SciQL, we take it a step further by providing an easy to use language feature to identify groups of cells based on their positional relationships. Each group forms a pattern, called a tile, which can be subsequently used to derive all possible incarnations for, e.g., statistical aggregation.

One way to evaluate SciQL is to confront the language design with a functional benchmark. Unfortunately, the area of array- and time series databases is still too immature to expect a (commercially) endorsed and crystallised benchmark. Instead, we exercise the SciQL design using well-chosen use cases in various scientific domains. In our previous paper [33], we have shown the expressiveness of SciQL in Landsat and astronomy image processing. In this paper, we use SciQL on a different class of array problems, namely time series. Time series play a significant role in many science areas, such as statistics, econometrics, mathematical finance, (digital) signal processing and all kinds of sensor data.

This paper is further organised as follows. Section 2 introduces SciQL through a series of examples. Section 3 demonstrates query functionality. Section 4 evaluates the language with a functional benchmark using seismological time series data. Section 5 discusses related work. Section 6 concludes the paper with a summary and an outlook on the open issues.
the default values. A cell is given a new value through an ordinary SQL UPDATE statement. A dimension can be used as a bound variable, which takes on all its dimension values (i.e., valid values of this dimension) successively. A convenient shortcut is to combine multiple updates into a single guarded statement. The evaluation order ensures that the first predicate that holds dictates the cell values. The refinement of the array is shown in the first query below. The cells receive a zero only in the case \( x = y \). The remaining queries demonstrate setting cell values in the arrays stripes, diagonal and sparse, respectively. The results are shown in Figure 2.

\[
\text{UPDATE matrix SET } v = \\
\quad \text{CASE WHEN } x > y \text{ THEN } x + y \text{ WHEN } x < y \text{ THEN } x - y \text{ ELSE } 0 \text{ END;}
\]

\[
\text{UPDATE stripes SET } v = x + y;
\]

\[
\text{UPDATE diagonal SET } v = v + 10;
\]

\[
\text{UPDATE sparse SET } v = \text{MOD(RAND()}, 14);\]

Assignment of a NULL value to an array cell leads to a 'hole' in the array, a place indistinguishable from the out of bounds area. Such assignments override any predefined DEFAULT clause attached to the array definition. For convenience, the built-in array aggregate operations SUM(), COUNT(), AVG(), MIN() and MAX() are applied to non-NULL values only.

Arrays can also be updated using INSERT and DELETE statements. Since all cells semantically exists by definition, both operations effectively turn into update statements. The DELETE statement creates holes by assigning a NULL value for all qualified cells. The INSERT statement simply overwrites the cells at positions as specified by the input columns with new values. Note that although the INSERT, UPDATE and DELETE statements do not change the existence of array cells, for unbounded arrays they may result in scaling the minimal bounding rectangle up/down. The three queries below together illustrate how to delete a column in the array matrix where \( x = 2 \), then shift the remaining columns, and (manually) set the last column of matrix to its default value. In the second and third queries, the \( x \) and \( y \) dimensions of the array matrix are matched against the projection columns of the SELECT statements. Cells at matching positions are assigned new values (see Figure 3).

\[
\text{DELETE FROM matrix WHERE } x = 2;
\]

\[
\text{INSERT INTO matrix SELECT } x-1, y, v \text{ FROM matrix WHERE } x > 2;
\]

\[
\text{INSERT INTO matrix SELECT } x, y, 0 \text{ FROM matrix WHERE } x = 3;
\]

### 2.3 Array and Table Coercions

One of the strong features of SciQL is to switch easily between a TABLE and an ARRAY perspective. Any array is turned into a corresponding table by simply selecting its attributes. The dimensions then form a compound primary key. For example, the matrix defined earlier becomes a table using the expression SELECT \( x \), \( y \), \( v \) FROM matrix or using a CAST operation like CAST(matrix AS TABLE). Note, that the semantics of an array leads to materialisation of all cells within the dimension bounds (or the minimal bounding rectangle for unbounded arrays), even if their values were set to a non-NULL default. A selection excluding the user specified default values may solve this problem.

An arbitrary table can be coerced into an array if the column list of the SELECT statement contains the dimension qualifiers '[' and ']'. A projection column, i.e., [\( \text{<expr>} \)]. Here, the \( \text{<expr>} \) is a <column name> or a value expression. For instance, let mtable be the table produced by casting the array matrix to a table. It can be turned into an array by picking the columns forming the primary key in the column list as follows: SELECT \( x \), \( y \), \( v \) FROM mtable, or using the reverse cast operation CAST(mtable AS ARRAY(\( x \),\( y \))). The result is an unbounded array with actual size derived from the dimension column expressions \( x \) and \( y \). The default values of all non-dimensional attributes are inherited from the default values in the original table.

### 3. QUERY MODEL

From a query’s perspective, querying a TABLE and an ARRAY are much alike. In both cases elements are selected based on predicates, joins, and groupings. The result of any query expression is a table unless the column list contains the dimension qualifiers ('[' and ']'). A novel way to use GROUP BY, called tiling, is introduced to improve structure based querying.

#### 3.1 Cell Selections

```
SELECT x, y, v FROM matrix WHERE v > 2;
SELECT [x], [y], v FROM mtable WHERE v > 2;
SELECT [T.k], [y], v FROM matrix JOIN T ON matrix.x = T.i;
```

The examples above illustrate a few simple array queries. The first query extracts values from the array matrix into a table. The second one constructs a sparse array from the selection, whose dimensional properties are inherited from the result set. The dimension qualifiers introduce a new dimension range, i.e., a minimal bounding box is derived from the result set, such that the answers fall within its bounds. The last query shows how elements of interest can be obtained from both arrays and tables using an ordinary join expression. It assumes a table \( T \) with two (or more) columns, where the column \( i \) is of a numeric type and the column \( k \) may be of any scalar type. The expression extracts the subarray from matrix and sets the bounds to the smallest enclosing bounding box defined by the values of the columns \( T.k \) and \( y \). The actual bounds of an array can always be obtained from the built-in functions MIN() and MAX() over the dimensions.

#### 3.2 Array Slicing

An ARRAY object can be considered an array of records in programming language terms. Therefore, the language supports positional index access conforming to the order the dimensions are introduced in the array definition. All attributes (dimensional and non-dimensional) of interest should be explicitly identified. A range pattern, borrowed from the programming language arena, supports easy slicing over individual dimensions using the aforementioned sequence pattern \( [<\text{start}>:<\text{step}>:<\text{stop}>] \). The range pattern is allowed in both the FROM and GROUP BY clauses. To illustrate this, we show a few slicing expressions over the arrays defined earlier (results are computed based on Fig. 2-a).

```
SELECT * FROM matrix[3][2];
-- yields: [3, 2, 5, 8]
SELECT v FROM matrix[1][1:3];
-- yields: [-1.0, -2.0, 0.0, -1.0, 3.0, 0.0, 4.0, 5.0]
```
The SQL UPDATE statement is extended to take array expressions directly. This leads to a more convenient and compact notation in many situations. The bounds of the subarray are specified by a sequence pattern of literals. Again, a sequence of updates acts as a guarded function. The array dimensions are used as bound variables that run over all valid dimension values. This is illustrated using the queries below:

```sql
UPDATE matrix SET matrix[0:2][*.v = v * 1.19;
UPDATE matrix SET matrix[x][*.v =
  CASE WHEN v < 0 THEN x WHEN v >10 THEN 10 * x ELSE 0 END;
```

### 3.3 Array Views

A common case is to embed an array into a larger one, such that a zero initialised bounding border is created, or to shift a vector before moving averages are calculated. To avoid possible significant data movements, the array VIEW constructor can be used instead. The first two queries below illustrate an embedding, i.e., to transpose and shift an array, respectively. In the SELECT clause, the `x` and `y` columns are used to identify the cells in the `vmatrix` to be updated. The last example illustrates how the aforementioned example of shift with zero fill of a column (see Section 2.2, second query group) can be modelled as a view. Note that the results of all SELECT statements in the examples below are tables, thus in the third query, the ordinary SQL UNION semantics applies.

```sql
CREATE VIEW ARRAY vmatrix (v INT DIMENSION[0:2:4][0:2:4]) AS
  SELECT x-1, y, v FROM matrix WHERE x > 2 UNION
  SELECT x, y, v FROM matrix WHERE x < 2;
```

```sql
CREATE VIEW ARRAY vector(x INT DIMENSION[0:2:4][0:2:4]) AS
  SELECT x, y, v FROM matrix WHERE x < 2 UNION
  SELECT x, y, v FROM matrix WHERE x > 2;
```

### 3.4 Aggregate Tiling

A key operation in science applications is to perform statistics on groups. They are commonly identified by an attribute or expression list in a GROUP BY clause. This value-based grouping can be extended to structural grouping for ARRAYS in a natural way. Large arrays are often broken into smaller pieces before being aggregated or overlaid with a structure to calculate, e.g., a Gaussian kernel function. SciQL supports fine-grained control over breaking an array into possibly overlapping tiles using a slight variation of the SQL GROUP BY clause semantics. Therefore, the attribute list is replaced by a parametrised series of array elements, called tiles. Tiling starts with an anchor point identified by its dimensional value(s), which is extended with a list of cell denotations relative to the anchor point. The value derived from a group aggregation is associated with the dimensional value(s) of the anchor point.

```sql
CREATE VIEW ARRAY vmatrix (x INT DIMENSION[-1:1:5],
  y INT DIMENSION[-1:1:5],
  v FLOAT DEFAULT 0.0 ) AS
  SELECT v FROM matrix[0:2:4][0:2:4];
```

A recurring operation is to derive check sums over array slabs. In SciQL this can be achieved with a simple tiling on, e.g., the x dimension. In this case, the anchor point is the value of `x`. For example:

```sql
SELECT [x], AVG(v) FROM matrix
GROUP BY matrix[x:x+2][y:y+2];
```

A discrete convolution operation is only slightly more complex. For, consider each element to be replaced by the average of its neighboring elements. The extended matrix `vmatrix` is used to calculate the convolution, because it ensures a zero value for all boundary elements. The aggregates outside the bounds `[0:4][0:4]` are not calculated by using an array slicing in the FROM clause.

```sql
SELECT [x], SUM(v) FROM matrix GROUP BY matrix[x][*];
```
It generates a listing of all columns with the distance from the refer-
values, which are used within the

tile selections. For this we simply need a table with dimension val-
functions, which are limited to aggregations over sliding windows
Using the dimension values in the grouping clause permits complex
ages, without the need to resort to self-joins. The following query
manipulations, such as interpolation and computing moving aver-
represents them as arrays indexed by the time stamps with a fixed

Using the dimension values in the grouping clause permits complex
structures to be defined. It generalises the SQL:2003 windowing functions, which are limited to aggregations over sliding windows
with static bounds and shift count over a sequence. The SciQL ap-
proach can be generalised to support the equivalent of mask-based
tile selections. For this we simply need a table with dimension val-
ues, which are used within the GROUP BY clause as a pattern to
search for.

4. TIME SERIES DATA PROCESSING

After introducing the main features of SciQL, we continue with
illustrating its expressiveness as a time series language. Generally
speaking, a time series is a sequence of data points with each point
attached a time stamp. A time series can be regular or irregular.
The data points in a regular time series are measured at successive
times spaced at uniform time intervals. In the sciences, sensor data
e.g., temperature, ground motion and strain gauges) is often a reg-
ular time series, as it comes in as a continuous stream at a fixed
rate. An irregular time series contains data points at successive
times spaced at arbitrary time intervals. Sensor data with gaps is
an irregular time series, in which the gaps typically indicate mal-
functioning sensors. In the time series domain there does not exist
a standardised functional test of expressiveness. Since the primary
target of SciQL is the scientific domains, we take the data from
seismology (an important scientific domain with a huge amount of
time series data) as a yardstick. In this section, we first discuss how
time series are supported by SciQL. Then we demonstrate how the
typical operations of seismic signal processing can be easily and
concisely phrased in SciQL.

4.1 Time Series

4.1.1 Fixed Time Series

If experiments are conducted at regular intervals, it is helpful to
represent them as arrays indexed by the time stamps with a fixed
stride. The SciQL language constructs allow for easy subsequent
manipulations, such as interpolation and computing moving aver-
ages, without the need to resort to self-joins. The following query
shows how SciQL is turned into a time series supporting language
by simply choosing a temporal domain for at least one dimension:

```
CREATE ARRAY ts1 |
  time TIMESTAMP DIMENSION[_TIMESTAMP '2011-01-01 09:00:00' : INTERVAL '1' MINUTE : * ]
  data FLOAT DEFAULT 0.0
);
```

The data type of the time dimension is a TIMESTAMP and its in-
crement is a temporal interval unit, e.g., a minute. This example
creates a fixed time series array. The two statements in the follow-
ing example are semantically identical, namely, they all populate
the array with five values starting from the first cell with a step size
of 2, overwriting the default values of these cells. Note, that they
explicitly identify the cells whose values should be overwritten.

```
INSERT INTO ts1 VALUES
  ('2011-01-01 09:00', 0.7793), ('2011-01-01 09:02', 0.9076),
  ('2011-01-01 09:04', 0.2267), ('2011-01-01 09:06', 0.2094),
  ('2011-01-01 09:08', 0.1295);
UPDATE ts1 SET ts1['2011-01-01 09:00'] = INTERVAL '2' MINUTE :
  ('2011-01-01 09:10').data =
  (0.7793), (0.9076), (0.2267), (0.2094), (0.1295);
```

Insertions with explicit time values may contradict the definition
of the time dimension. If the value is before start or after stop,
the insertion is ignored. If the value is inside of the [start, stop] interval, but does not match any of the values defined by
the temporal unit step, we apply gridding. That is, the data value
will be inserted into a cell which dimensional values are the clos-
est to the original timestamp. In the following query, the value of
47.00008 seconds will be rounded to 1 minute, so that the value
0.9216 is inserted into the cell with dimensional value of '2011-01-
01 09:01':

```
INSERT INTO ts1 VALUES ('2011-01-01 09:00:47.00008', 0.9216);
```

4.1.2 Unbounded Time Series

In many cases not all constraints of a time dimension are known
in advance. For instance, a time series of the waveforms produced
by a seismic sensor may only have a start time stamp but no stop
time stamp, because once the measurement has started, it continues
as long as possible. Moreover, sensor data often contains time gaps
even if the sample rate is known beforehand, so it might not be
desirable to enforce a step size in such time series, which can cause
losing information about the gaps. This is where time series with
unbounded (time) dimensions come in handy. The examples below
show several variants of the ts1 defined above with some or all of
the constraints start, step or stop omitted. The arrays ts3, ts4, and ts5 do not carry a step size, which means that any event
time stamp up to a microsecond difference would be acceptable
(microsecond is the smallest unit for a time stamp in SQL:2003).
The dimensions here merely enforce an event order.

```
CREATE ARRAY ts2 |
  time TIMESTAMP DIMENSION[_TIMESTAMP '2011-01-01 09:00:00' :
    INTERVAL '1' MINUTE : * ]
  data FLOAT DEFAULT 0.0
);
```

```
CREATE ARRAY ts3 |
  time TIMESTAMP DIMENSION[_TIMESTAMP '2011-01-01 09:00:00' :
    TIMESTAMP '2011-01-01 10:00:00'],
  data FLOAT DEFAULT 0.0
);
```

```
CREATE ARRAY ts4 |
  time TIMESTAMP DIMENSION[_TIMESTAMP '2011-01-01 10:00:00'; * : *]
  data FLOAT DEFAULT 0.0
);
```

```
CREATE ARRAY ts5 |
  time TIMESTAMP DIMENSION,
  data FLOAT DEFAULT 0.0
);
```
Compared with fixed time series, inserting values into an unbounded time series without explicitly specifying the cell indices has several semantic differences. Basically, the values can be inserted at any positions satisfying the partial constraints of the time dimension in the array definition, as long as the relative order among the values is preserved. However, this operation can be made more deterministic by using the available constraints. Unbounded time series can be divided into the following classes, based on the absent dimension constraint(s):  

1. One end of the dimension range (i.e., `start` or `stop`);  
2. Both ends of the dimension range;  
3. The step size;  
4. One end of the dimension range and the step size;  
5. All constraints.

The first class is easy to handle. Consider the query:

```sql
INSERT INTO ts2 VALUES
((0.7793), (0.9076), (0.2267), (0.2094), (0.1295));
```

Since the array `ts2` has a `start` and `step` for its time dimension, the values are inserted into the first five cells of the array (if the `start` was omitted, the last five cells are chosen), i.e., at the timestamps `'2011-01-01 09:09:00'`, `'2011-01-01 09:01:00'`, . . . , `'2011-01-01 09:04:00'`, overwriting any existing values at these positions. If both ends of the dimension ranges are omitted (class `ii`), we take the current time `now()`, rounded to the granularity of the step size, as the starting position for insertions. When the step size is omitted (class `iii`), we use the smallest unit of the dimension data type as the default step size. In case of `timestamp`, it is the microsecond. Thus, the query:

```sql
INSERT INTO ts3 VALUES
((0.7793), (0.9076), (0.2267), (0.2094), (0.1295));
```

produces the time series `('2011-01-01 09:00:00.000000', 0.7793), . . . , ('2011-01-01 09:04:00.000000', 0.1295)`.

To handle the unbounded time series of the classes `iv`) and `v)`, we combine the rules used for the first three classes. For instance, to handle the query:

```sql
INSERT INTO ts5 VALUES
((0.7793), (0.9076), (0.2267), (0.2094), (0.1295));
```

we take the value of `now()` as the start position and microsecond as the step size.

### 4.1.3 Interpolation

Applications often assume values at regular time intervals, while the available measurement time series may have gaps of missing values or values taken at irregular time intervals. In such cases interpolation can be used to provide approximate values at regular time steps. Consider the irregular time series `ts4` set by the following query:

```sql
INSERT INTO ts4 VALUES
('2011-01-01 09:09:00', 0.28), ('2011-01-01 09:02:00', 0.36),
('2011-01-01 09:05:00', 0.52);
```

The interpolation can be formulated in SciQL as follows. First, we create a fixed time series with the desired regular step, for instance 1 minute:

```sql
CREATE ARRAY heartbeat |
  time TIMESTAMP DIMENSION
  (TIMESTAMP '2011-01-01 09:00' : INTERVAL '1' MINUTE :
     TIMESTAMP '2011-01-01 10:00'),
  data FLOAT DEFAULT NULL
};
```

The next step is to compute and insert the interpolated values at the regular time steps. To make the discussion concrete, we will use linear interpolation to compute the approximate data values:

```sql
INSERT INTO heartbeat
  SELECT hb.time,
    irr.data + (hb.time - irr.time) *
    (irr[NEXT(irr, irr.time)].data - irr.data) / (NEXT(irr, irr.time) - irr.time)
  FROM heartbeat AS hb, ts4 AS irr
  WHERE hb.time >= irr.time AND hb.time <= NEXT(irr, irr.time);
```

The above query matches the time value in the regular time series with the nearest preceding and following values in the time dimension of the irregular time series. The built-in function `NEXT()` takes an array name and a value for each of its dimension, only one in this example, and returns the nearest following value in the major dimension of the array. The time series `heartbeat` contains the non-NULL values: `('2011-01-01 09:00', 0.28), ('2011-01-01 09:01', 0.32), ('2011-01-01 09:02', 0.36), ('2011-01-01 09:03', 0.413), ('2011-01-01 09:04', 0.466), ('2011-01-01 09:05', 0.52)`. Note, that the data values will remain `NULL` outside of the time interval covered by the irregular time series.

### 4.2 Seismic Use Cases

In seismology, SEED (Standard for the Exchange of Earthquake Data) [48] is the most widely used international standard file format for the exchange of waveform data among global broadband seismograph networks. The SEED standard defines a format for digital data measured at one point in space and at equal intervals of time. A SEED volume consists of a number of ASCII control headers followed by a number of binary data records, i.e., the waveform time series. The control headers contain, among others, all the configuration and identification information for the station and all its instruments, and meta information of the data records stored in this SEED volume. Each data record contains both a raw waveform data stream produced by one station and auxiliary information of this data stream, e.g., start time and sample rate. In SciQL, all waveform data streams from multiple stations can be stored in one two-dimensional array, as shown below. For simplicity, we assume each station produces one waveform data stream. In reality, a seismic station contains three channels (to measure the ground movement in three different directions) with each channel producing one waveform data stream. Separating data streams from different channels merely adds one more integer dimension in the array `MSeed`.

```sql
CREATE ARRAY MSeed |
  station VARCHAR(5) DIMENSION['O' : * : 'ZZZZZ'],
  time TIMESTAMP DIMENSION,
  data FLOAT
};
```

Since each seismic station has an unique identifier consisting of up to five characters (upper case letters and the digits 0 – 9), the station `IDs` is denoted using an unbounded dimension of the type `VARCHAR`, which uses the lexical order. Finally, an unbounded `time` dimension is defined for the waveform data. The `time` dimension does not carry any constraints, because each waveform data stream can have a different start/stop time and sample rate, a station can change its sampling rate over time, and the waveform data can have arbitrary time gaps.

The meta data in the SEED volume is stored in normal tables, of which an excerpt is shown below. The `station` dimension in the `MSeed` array also acts as foreign keys pointing to the tables where the meta data is stored (not all attributes are shown):
4.2.1 Events Detection

When studying seismic data, one of the first information a seismologist wants to obtain is whether the waveform contains any interesting seismic events, and then cut off short pieces of the waveform (e.g., 3 minutes) around the events for further analysis. One method to detect seismic events is based on the ratio of Short Term Averaging / Long Term Averaging, e.g., STA of 2 seconds and LTA of 15 seconds. To reduce noise the mean of each time series in MSeed is first removed. The query below subtracts from each data point in the array MSeed the mean of its containing time series. Inserting the new value into the same cell in MSeed overwrites the existing value.

```
INSERT INTO MSeed
SELECT station, time, (data - AVG(MSeed[station][*].data)) AS data
FROM MSeed;
```

The next step, computing the STA/LTA ratio, is straightforward with the SciQL tiling feature. If the ratio is larger than the threshold \( \delta \), a tuple is added to the Event table:

```
CREATE TABLE Event (  
id INT NOT NULL UNIQUE AUTO_INCREMENT,  
station VARCHAR(5) PRIMARY KEY,  
time TIMESTAMP,  
ratio FLOAT,  
PRIMARY KEY (station, time) );
```

Insertion into the Event table follows:

```
INSERT INTO Event
SELECT station, time, ratio
FROM MSeed;
```

In the remainder of this section we illustrate the expressiveness of SciQL using several essential operations in seismic data analysis, such as event detection, cross-correlation, and convolution.

4.2.2 Digital Signal Processing

Cross-correlation, convolution and Fourier transformation are fundamental operations in (seismological) Digital Signal Processing (DSP) [54]. They are provided as standard functions in many mathematical libraries, such as Matlab, Octave and Sage. Those functions can be easily hooked up in SciQL as external UDFs. However, to better utilise the query processing and optimisation facilities of DBMSs, one should be able to directly phrase these operations in SQL. In SciQL this is easy, as all necessary features are present.

**Cross-correlation** is one of the most commonly used operations in seismology, much like the join operations in database systems. In DSP, cross-correlation measures the similarity of two waveforms whenever the two sequences intersect, compute the product of all intersecting values and sum all products up. Figure 6 shows an example of computing the cross-correlation of two waveforms containing respectively 4 and 3 items. In SciQL, \( f \star g \) can be expressed as shown below. The query assumes two one-dimensional arrays \( F \) and \( G \) of real numbers, their cross-correlation is defined as:

\[
(f \star g)[n] \overset{\text{def}}{=} \sum_{m=-\infty}^{\infty} f[n+m]g[n] = \langle f \rangle \langle g \rangle = \text{cov}(f, g)
\]

Unfortunately, the events detected by this simple STA/LTA algorithm contain many events not associated to an earthquake (they could have been caused by a cow passing by). The false positives have to be filtered out. This can be done by checking events detected by neighbouring stations (see table Neighbours below), because a real seismic event should be detected by multiple stations with time delays within some known ranges (i.e., between mindelay and maxdelay) and some strength reduction of the seismic wave (i.e., weight).
each cell of CrCorr, the query takes the intersecting slices of \( F \) and \( G \) (in the GROUP BY clause) to compute the products and sum. The built-in functions \( \text{MIN()} \) and \( \text{MAX()} \) return the smaller/larger value of its two parameters, which are used to prevent array slicing from going out of the dimension bounds.

```
DECLARE n INT;
SET n = -fmax;
CREATE ARRAY CrCorr {
  idx INT DIMENSION[fmin:1:fmax],
  val FLOAT DEFAULT 0.0
};
INSERT INTO CrCorr
SELECT C.idx, SUM(F.val * G.val)
FROM Fr, G, Conv AS C
GROUP BY F[MAX(gmin, C.idx) : MIN(gcnt, fcnt+C.idx)];
```

Computing the convolution of two sequences \( f \ast g \) is another important operation in seismology. It is used in, e.g., design and implementation of Finite Impulse Response filters in DSP. Convolution differs from cross-correlation only in one step, namely, the sequence \( f \) is first reversed before it is sliced. Sequence reversing in SciQL is captured by a slicing with negative step size, stored as an array view Fr. The following query computes the convolution of \( f \) and \( g \) and stores the results in Conv (variables are borrowed from the cross-correlation example).

```
CREATE VIEW ARRAY Fr (pos INT DIMENSION[min1:max], val FLOAT)
AS
SELECT val FROM F[maxf-1:maxf];
```

The discrete Fourier transform (DFT) is a mathematical operation that transforms a discrete sequence in the time domain into its frequency domain representation. Since the output (sequence) of a DFT always contains complex numbers, a data type not supported by SQL:2003, we discuss here how the real DFT can be written in SciQL. The real DFT is a version of the discrete Fourier transform that uses real numbers to represent both the input and output signals. Given a sequence of \( N \) real numbers \( x[i] \), where \( i = 0, \ldots, N-1 \), the real DFT transforms it into two sequences of \( N/2 \) real numbers \( \Re X[k] \) and \( \Im X[k] \), where \( k = 0, \ldots, N/2 \).

\[
\Re X[k] = \sum_{i=0}^{N-1} x[i] \cos(2\pi k i / N), \quad \Im X[k] = -\sum_{i=0}^{N-1} x[i] \sin(2\pi k i / N)
\]

That is, the real DFT decomposes signals \( x[i] \) in time domain into a sine wave \( \Im X[k] \) and a cosine wave \( \Re X[k] \) in frequency domain. This formula can be directly expressed in SciQL. Consider the array \( f \) defined above, the query below computes its real DFT transformation into the cosine wave \( \Re X[k] \). The results are stored in the new array DFTRe, which has an integer dimension with values of \( k \) representing the frequencies.

```
DECLARE n INT;
SET n = -fmax;
CREATE ARRAY DFTRe {
  k INT DIMENSION[0:N/2+1],
  val FLOAT DEFAULT 0.0
};
INSERT INTO DFTRe
SELECT k, SUM(F.val * \cos(2*PI()*k*pos/N))
FROM DFTRe AS D, F
GROUP BY D[k], F[*];
```

In this section, we discussed ways to represent time series with different properties and showed how routine DSP operations on time series can be formulated in SciQL. Although the operations addressed are not exhaustive, they are sufficient to show the power of SciQL in array oriented data processing. The structural grouping feature provides large flexibility to carve out a slab of an array for further processing. Note that we only concentrate on querying time series at the language level. Efficient processing of the queries discussed is part of ongoing implementation work. For instance, Fast Fourier Transform algorithms [9] should be considered to speed up the DFT computation.

5. RELATED WORK

The need for convenient data management systems to efficiently store, query and manipulate scientific data has been generally recognized. Much research has been done on identifying the specific requirements of scientific data management and the missing features that keep the scientists from using DBMS. Already in the 80’s, Shoshani et al. [52] identified common characteristics among the different scientific disciplines. The subsequent paper [53] summarizes the research issues of statistical and scientific databases, including physical organisation and access methods, operators and logical organization. Application considerations led Egenhofer [17] to conclude that SQL, even with various spatial extensions, is inappropriate for the geographical information systems (GIS). Similar observations were made by e.g., Davidson in [14] on biological data. Maier et al. [39] injected “a call to order” into the database community, in which the authors stated that the key problem for the relational DBMSs to support scientific applications is the lack of support for ordered data structures, like multidimensional arrays and time series. The call has been well accepted by the community, considering the various proposals on DBMS support (e.g., [6, 8, 56, 12, 21, 34, 50]), SQL language extensions (e.g., [5, 35, 45]) and algebraic frameworks (e.g., [12, 56, 37, 41]) for ordered data.

The precursors of SQL:1999 proposals for array support focused on the ordering aspect of their dimensions only. Examples are the sequence languages SEQUIN [50] and SRQL [45]. SEQUIN uses the abstract data type functionality of the underlying engine to realize the sequence type. SRQL is a successor of SEQUIN which treated tables as ordered sequences. SRQL extends the SQL FROM clauses with GROUP BY and SEQUENCE BY to group by and sort the input relations. Both systems did not consider the shape boundaries in their semantics and optimisation schemes. AQuery [35] inherits the sequence semantics from SEQUIN and SRQL. However, while SEQUIN and SRQL kept the tuple semantics of SQL, AQuery switched to a fully decomposed storage model.

Query optimisation over array structures led to a series of attempts to develop a multidimensional array-algebra, e.g., AML [41], AQL [37] and RAM [56]. Such an algebra should be simple to reason about and provide good handles for efficient implementations. AML focuses on decomposing an array into slabs, applying functions to their elements, and finally merging slabs to form a new...
array. AQL is an algebraic language with low-level array manipulation primitives. Four array-related primitives (two for creation, one for subscribing and one for determining shapes) plus auxiliary features, e.g., conditionals and arithmetic operations, allow application-specific array operations to be defined within AQL. The user specifies an algebraic tree with embedded UDF calls. Neither AML nor AQL provides a declarative mechanism to define the order the queries manipulate data. Comparing with array algebras, SciQL has a much more intuitive approach where the user focuses on the final structure.

RAM [56] is a proposal for flexible representation of information retrieval models in a single multidimensional array framework. It introduces an array algebra language on top of MonetDB [7] and is used as the “gluing layer” for DB+IR applications. RAM defines a set of basic array algebra operators, including MAP, APPLY, AGGREGATE, CONCAT, etc. Queries in RAM are compiled by the front-end into an execution plan to be executed by the MonetDB kernel. RAM does not support a declarative language such as SQL.

SRAM [12] is a following up of RAM that pays special attention to efficient storing and querying of sparse arrays in relational DBMS. Despite the abundance of research effort, few systems can handle sizable arrays efficiently. A good example is RasDaMan [6], which is a domain-independent array DBMS for multidimensional arrays of arbitrary size and structure. It has been completely designed in an object-oriented manner. It follows the classical two-tier client/server architecture with query processing done completely within the server. Arrays are decomposed into chunks, which form the unit of storage and access. The chunks are stored as BLOBS, so (theoretically) it can be ported to any DBMS supporting BLOBS. The RasDaMan server acts as a middleware, mapping the array semantics to a simple “set of BLOB” semantics. RasDaMan provides an SQL-92 based query language RasQL [5] to manipulate raster images using foreign function implementations. It defines a compact set of operators, e.g., MARRAY creates an array and fills it by evaluating a given expression at each cell; CONDENSE aggregates cell values into one scalar value; SORT slices an array along one of its axes and reorders the slices. RasQL queries are executed by the RasDaMan server, after the necessary BLOBS have been retrieved from the underlying DBMS.

The approaches taken by RAM and RasDaMan have a common drawback: arrays are black boxes to the underlying DBMS. This means that RAM and RasDaMan cannot fully benefit from the query execution facilities provided by the underlying DBMS. Contrary, the underlying DBMS is not aware of the specific array properties, missing opportunities for query optimization.

A recent attempt to develop an array database system from scratch is undertaken by the SciDB group [55]. Its mission is the closest to SciQL, namely, building an array DBMS with tailored features to fit exactly the need of the science community. The work of SciDB has focused on an efficient distributed architecture for array query processing ([13], [8]), in which arrays are vertically partitioned and divided into overlapping chunks (or slabs). At the language level, SciDB (version 0.75) supports both a declarative Array Query Language (AQL) and an Array Functional Language (AFL) [46](note that SciDB’s AQL is unrelated with the earlier work on the algebraic language AQL [37]). AQL supports a subset of SQL features with extensions allowing creating arrays with named dimensions. Only integer typed dimensions are supported and the users should specify how the array should be divided into chunks when creating an array. Most array manipulation features are defined in the AFL by means of functional operators, e.g., SLICE, SUBSAMPLE, SJOIN, FILTER and APPLY. Compared with AQL and AFL, SciQL takes language design a step further by proposing a seamless integration with SQL:2003 syntax and semantics.

Various database researchers have embarked on scientific applications that call for an array query language. PostgreSQL allows columns of a table to be defined as variable-length multidimensional array. Arrays of built-in type, enum type, composite type and user-defined base type can all be created. Basic arithmetic operators on arrays and simple slicing, i.e., integer indexes always increased by 1, are supported. Unfortunately, PostgreSQL has followed the SQL standard to use anonymous dimensions, a limitation that has been disputed by the science community [47]. AQuery [35] integrates table and array semantics into one kind of ordered entities arrables, a.k.o column store where the index is kept. An arrable’s ordering can be defined at creation time using an ORDERED BY clause, which can be also altered per query, using an ASSUMING ORDER clause. Array access is supported with a few functions, e.g., first(<N>, <col>) and last(<N>, <col>).

Much research work has been done on time series data processing in the areas such as financial statistics [40, 18], (multimedia) image processing [30] and data mining [2, 30, 29]. Existing research work has been focused on algorithms for, e.g., similarity searching (using distance algorithms) [10, 25, 57, 11, 16, 1], pattern detection or matching [44, 19, 59, 28, 24], classification [58, 3, 36, 26], indexing [51, 31, 57] and compressing [18, 27, 32]. Our work at the language level is orthogonal to the existing techniques for, e.g., similarity searching, pattern matching and classification, while we might benefit from existing work on indexing and compressing when implementing SciQL. Nevertheless, many issues are still left open. Very little work has been done on using DBMSs for time series data processing, because it has been generally realised that scientific operations are difficult to be expressed in SQL and inefficient to evaluate [15, 49]. Existing techniques have in general only shown their usefulness for small time series [38], [51] might be the only work that tries to tackle time series towards terabytes (up to 750GB). Thus, it is unknown how well the existing techniques will perform when dealing with terabytes and larger scale of time series.

6. SUMMARY AND FUTURE WORK

In this paper we have introduced SciQL, a query language for scientific applications and its use in querying time series. SciQL has been designed to lower the entry fee for scientific applications to use a database system. The language stands on the shoulders of many earlier attempts. SciQL preserves the SQL:2003 flavor using a minimal enhancements to the language syntax and semantics. Convenient syntax shortcuts are provided to express array expressions using a conventional programming style. We illustrated the needs for array-based query capabilities in the seismic waveform data processing. The concise description in SciQL brings relational and array processing symbiosis one step closer to reality. Future work includes development of a formal semantics for the array extensions, development of an adaptive storage scheme and exploration of the performance on functionally complete science applications. A prototype implementation of SciQL within the MonetDB [43] framework is being under development.

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7. REFERENCES


